

ISE-INFORMS Research Seminar

Buffered Probability of Exceedance (bPOE): Mathematical Properties and Applications

SPEAKER INFORMATION

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Dr. Uryasev is director of the Risk Management and Financial Engineering Lab and director of the PhD Program with Concentration in Quantitative Finance at the University of Florida. His research is focused on efficient computer modeling and optimization techniques and their applications in finance and military projects. He published three books (monograph and two edited volumes) and more than 130 research papers. He is a co-inventor of the Conditional Value-at-Risk and the Conditional Drawdown-at-Risk optimization methodologies. He is developing optimization software in risk management area: VaR, CVaR, Default Probability, Drawdown, Credit Risk minimization.

SEMINAR Session INFORMATION

DATE: MONDAY, April 10

TIME: 12:15pm

LOCATION: Durham 260

PROVIDED: Pizza and Soda

Abstract: The Probability of Exceedance (POE) is frequently used to measure uncertainties in outcomes. For instance, POE is used to estimate probability that assets of a company fall below liabilities. POE measures only the frequency of outcomes and ignores magnitude of outcomes. POE counts outcomes exceeds the threshold, and it “does not worry” about the amount by which each outcome exceeds the threshold. POE is lumping together all threshold exceedance events, potentially “hiding” quite large and very troublesome outcomes. Moreover, POE has poor mathematical properties when used to characterize discrete distributions of random values (e.g., when distributions are defined by observed historical data). POE for discrete distributions is a discontinuous function of control variables, making it difficult to analyze and optimize.

This presentation discusses a new probabilistic characteristic called Buffered Probability of Exceedance (bPOE). With bPOE, it is possible to count outcomes close to a threshold value, rather than only outcomes exceeding the threshold. To be more precise, bPOE counts tail outcomes averaging to some specific threshold value. For instance, 4% of land-falling hurricanes in US have cumulative damage exceeding \$50 billion (i.e., $POE = 0.04$ for threshold=\$50 billion). It is estimated, that the average damage from the worst 10% of hurricanes is \$50 billion. In terms of bPOE, we say $bPOE=0.1$ for threshold=\$50 billion. bPOE shows that largest damages having magnitude around \$50 billion have frequency 10%. bPOE can be considered as an important supplement to POE. We think that bPOE should be routinely calculated together with POE. This example shows that bPOE exceeds POE, which is why it is called Buffered Probability of Exceedance. The positive difference, $bPOE-POE$, can be interpreted as some “buffer.” The bPOE concept was recently developed as an extension of Buffered Probability of Failure (introduced by Rockafellar and Royset). bPOE has been derived from Conditional Value-at-Risk (CVaR) characteristic of uncertainty. Actually, bPOE is an inverse function of CVaR and it inherits a majority of the exceptional mathematical properties of CVaR (which is a so called “coherent measure of risk”). Similar to CVaR, minimization of bPOE can be reduced to convex and Linear Programming.

We will discuss two applications of bPOE concept. The first application considers the Cash Matching of a Bond Portfolio. We minimize bPOE that assets exceed liabilities. The second application uses bPOE in data mining. Currently, the Area Under the Receiver Operating Characteristics Curve (AUC) is standardly used to evaluate classification models. AUC can be presented as the probability that some discrete random value is below zero. We explored so called Buffered AUC (bAUC) as a counterpart of the standard AUC.

Faculty and Students are invited